



Formal Verification of Cryptographic Protocols

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ProVerif slides are based on Blanchet & Cheval's documentation

Motivation

- Ignored implementation details
- Use of obsolete modes
- Need for a synchronous automatic check
- Handling concurrent and serial processes.

Projects

- ProVerif: Automated tool for verification using a classic symbolic model (Dolev-Yao).
- CryptoVerif: Mechanical verification using computation proofs.
- Tamarin Prover: Heuristic, deduction and equational reasoning.
- F*: Type-checker using SMT (satisfiability modulo theories) and manual proofs (Ocaml..)

- Deepsec: Bounded number of sessions, security properties expressed as trace equivalences.
- Scyther: Inference for proving or disproving a protocol.
- CertiCrypt: Coq-based for mechanised proofs in a computational model.
- EasyCrypt: Uses SMT and axiomatic rules to improve CertiCrypt timing.

Pi-calculus syntax

• $N = \{a, b, c, d, \dots\}$ interconnection names

• $P ::= 0$ null process

output

• $a(x).P$ input

• $P \mid P$ parallel

- $\nu x. P$ restriction
- $! P$ replication
- $P + P$ sum/choice
- $|a(x).Q \Rightarrow P|Q \{b/x\}$ communication

Proverif Internal Mechanism

- 1- Processes
- 2- Horn Clauses
- 3- Saturation
- 4- Verification using all lemmas and axioms.

ProVerif Initiation

On command line: ./proverif [options] <filename>

Script:

(* This is a comment*)

free c : channel.

free RSA: bitstring [**private**].

query attacker (RSA) .

Process

out (c ,RSA) ;

0

Process 0 (that is, the initial process):
{1}out(c, RSA)

-- Query not attacker(RSA[]) in process 0.
Translating the process into Horn clauses...
Completing...
Starting query not attacker(RSA[])
goal reachable: attacker(RSA[])

Derivation:

1. The message RSA[] may be sent to the attacker at output {1}.
attacker(RSA[]).
2. By 1, attacker(RSA[]).
The goal is reached, represented in the following fact:
attacker(RSA[]).

A more detailed output of the traces is available with
set traceDisplay = long.

out(c, ~M) with ~M = RSA at {1}

The attacker has the message ~M = RSA.
A trace has been found.
RESULT not attacker(RSA[]) is false.

Verification summary:

Query not attacker(RSA[]) is false.

- ProVerif tests the query `not attacker(RSA)`, it is true when the name is not derivable by the attacker.
- The attacker has, however, been able to obtain the free name `RSA` as denoted by the `RESULT not attacker:(RSA[])` is false.
- ProVerif is also able to provide an attack trace:

`out(c, ~M)` with $\sim M = \text{RSA}$ at `{1}`

The attacker has the message $\sim M = \text{RSA}$.

Operations

- Constructors are used to build terms: $f()$ for instance, a shared-key encryption would be denoted by:

fun senc(bitstring, key) : bitstring.

- Destructors use rewrite rules $g() \ M$.

let $x = g()$ **in** P **else** Q

It can be seen in decryption:

fun senc(bitstring, key) : bitstring
reduc forall $m : \text{bitstring}, k : \text{key}; \text{sdec}(\text{senc}(m, k), k) = m$.

In other words,

- for each constructor f of arity n , the clause

$$att() \wedge \dots \wedge att() \Rightarrow att(f(\dots,))$$

is generated, representing that the adversary can compute $f(\dots,)$ by applying f

when it has $, \dots, .$

For instance, for shared-key encryption $senc$, the following clause is generated:

$$att(m) \wedge att(k) \Rightarrow att(senc(m, k))$$

- For each destructor g , defined by a rewrite rule $g(\dots) \rightarrow M$, the clause $att() \wedge \dots \wedge att() \Rightarrow att(M)$

is generated, representing that the adversary can compute M when it has \dots , by applying g .

For instance, for shared-key decryption $sdec$, defined by $sdec(senc(m, k), k) \rightarrow m$, the following clause is generated:

$$att(senc(m, k)) \wedge att(k) \Rightarrow att(m)$$

If the adversary has the ciphertext $senc(m, k)$ and key k , it can obtain the cleartext m by decryption.

Denning-Sacco Protocol

Message 1. $A \rightarrow B : \{\{k\}_{sk_A}\}_{pk_B} \quad k \text{ fresh}$

Message 2. $B \rightarrow A : \{s\}_k$

$\text{new } sk_A.\text{new } sk_B.\text{let } pk_A = \text{pk}(sk_A) \text{ in let } pk_B = \text{pk}(sk_B) \text{ in}$
 $\text{out}(c, pk_A).\text{out}(c, pk_B).$

(A) $! \text{in}(c, x_{pk_B}).\text{new } k.\text{out}(c, \text{aenc}(\text{sign}(k, sk_A), x_{pk_B})).$

$\text{in}(c, x).\text{let } s = \text{sdec}(x, k) \text{ in } 0$

(B) $\parallel ! \text{in}(c, y).\text{let } y' = \text{adec}(y, sk_B) \text{ in}$

$\text{let } k = \text{check}(y', pk_A) \text{ in out}(c, \text{senc}(s, k))$

Thank you.

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