The Lean standard library

Markus Himmel, Lean FRO

Formal mathematics

- Formal mathematics
- Software and hardware verification

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- (Verified) software development

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- Al research for mathematics and code synthesis

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- Software and hardware verification
- (Verified) software development
- Al research for mathematics and code synthesis
- New math and computer science education methodologies

• The language (parser, elaborator, kernel, compiler, runtime, ...)

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- Tactics (basic like exact or rewrite, advanced like grind or bv_decide)
- The metaprogramming framework
- The standard library

It's what makes Lean into a **general-purpose** programming language.

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It's what makes Lean into a verification platform.

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It is a public API.

- 1. Core types and operations
 - a. Basic types
 - b. Numeric types, including floating point numbers
 - c. Containers
 - d. Strings and formatting
- 2. Language constructs
- 3. Libraries
- 4. Operating system abstractions

- 1. Core types and operations
- 2. Language constructs
 - a. Ranges and iterators
 - b. Comparison, ordering, hashing and related type classes
 - c. Basic monad infrastructure
- 3. Libraries
- 4. Operating system abstractions

- 1. Core types and operations
- 2. Language constructs
- 3. Libraries
 - a. Random numbers
 - b. Dates and times
- 4. Operating system abstractions

- 1. Core types and operations
- 2. Language constructs
- 3. Libraries
- 4. Operating system abstractions
 - a. Concurrency and parallelism primitives
 - b. Asynchronous I/O
 - c. FFI helpers
 - d. Environment, file system, processes
 - e. Locales

All Lean users!

Programmers

- Programmers
 - Programmers writing verified software

- Programmers
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 - Metaprogrammers

- Programmers
 - Programmers writing verified software
 - Metaprogrammers
 - Lean developers

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 - Lean developers
 - Library authors

- Programmers
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 - Metaprogrammers
 - Lean developers
 - Library authors
- Mathlib users

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- Programmers
 - Programmers writing verified software
 - Metaprogrammers
 - Lean developers
 - Library authors
- Mathlib users
- Software and hardware verification users
- Individuals evaluating Lean for use

Useful for real applications

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High-quality and polished: comprehensive, consistent, systematic, optimized, verified, testable, tested, documented, interconnected, stable, comprehensible, visible, benchmarked, ...

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Excellent **out-of-the-box experience** for software development and software verification

End goal: make formal verification economical and commonplace

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Challenge: things don't just need to be possible, but easy and productive

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No missing material

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- No inconsistencies or other papercuts

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Need a principled approach to quality!

Tooling and processes lead to fewer mistakes: CI, linters, code review.

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There are gaps!



Quality assurance will always have a manual component

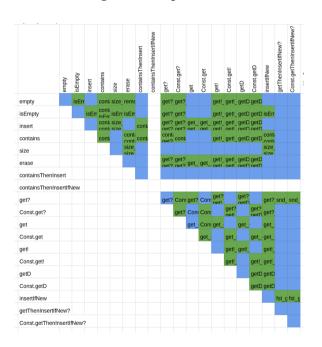
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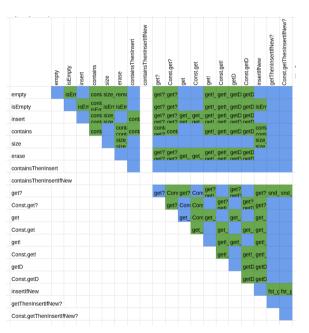
- Quality assurance will always have a manual component
- Not all rules can be fully formalized, and many rules will have exceptions
- Global consistency of the library is desirable
- To understand where we are, we need to be able to visualize and track the state of the library

Early experiments

Early experiments

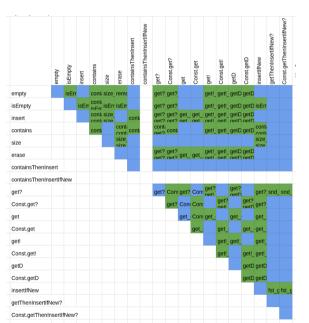


Early experiment



A	В	C	D	E	F
"PlainTime", "PlainDate", "PlainDateTim	e", Std.Time.Pla	aiı Std.Time.Pi	la Std.Time.PlainD.	Std.Time.ZonedDa	Std.Time.DateTime
PlainTime	x				
PlainDate		X			
PlainDateTime			×		
ZonedDateTime				x	
DateTime					x
addNanoseconds	x		X	X	X
addMilliseconds	X		X	x	X
addSeconds	X		X	X	X
addMinutes	X		×	x	X
addHours	X		×	X	X
addDays		X	X	x	X
addWeeks		X	X	X	X
addMonthsClip		X	X	X	X
addMonthsRollOver		X	X	X	X
addYearsClip		X	X	x	X
addYearsRollOver		X	X	x	X
alignedWeekOfMonth		X	×		X
atDate	х	^	×		^
atTime	^	×	X		
nano		^	^		
India	x		x	х	?
nanosecond millisecond	X		X	X	?
miniscond					
minute	X		X	X	X
accond	X		×	X	X
noui	Х		×	X	X
day		Х	х	х	Х
weekOfMonth		X	X	X	Х
weekOfYear		Х	X	Х	X
weekday		X	X	X	X
month		Х	X	X	X
quarter		X	X	X	X
year		X	X	Х	X
era		X	X	X	X
convertZoneRules				X	
date			×	x	X
time			x	х	?
format	Х	X	X	x	X
fromLeanTime24Hour	х				
fromTime12Hour	х				
fromTime24Hour	x				
fromAmericanDateString		x			
fromLeanDateString		X			
fromSQLDateString		x			
fromAscTimeString			×		x
fromDateTimeString			X		
fromLeanDateTimeString			x		
fromLongDateFormatString			×		x
fromDateTimeWithZoneString				х	
fromDateTimeWithZoneString fromISO8601String				X	
fromLeanDateTimeWithZoneString				x	
fromRFC822String				×	
fromRFC850String				×	
fromRFC850String toLeanTime24Hour	x			^	
toTime12Hour	X				
toTime24Hour	Х				

Early experiments



A	В	С	D	E	F
"PlainTime", "PlainDate", "PlainDateTime",	Std.Time.Plai	Std.Time.Pl	Std.Time.PlainD	a Std.Time.ZonedD	a Std.Time.DateTime
PlainTime	х				
PlainDate		X			
PlainDateTime			×		
ZonedDateTime				х	
DateTime					×
addNanoseconds	x		x	х	×
addMilliseconds	x		x	х	×
addSeconds	x		X	X	×
addMinutes	х		×	х	×
addHours	x		X	X	×
addDays		X	x	x	×
addWeeks		X	x	x	X
addMonthsClip		X	X	X	X
addMonthsRollOver		X	X	X	X
addYearsClip		X	×	X	X
addYearsRollOver		X	x	X	X
alignedWeekOfMonth		X	×		X
atDate	х		x		
atTime		×	×		
nano		^	^		
nanosecond	х		×	x	?
millisecond	X		×	x	?
minute	X		X	x	X
second	X		X	x	x
hour	X		X	x	X
day	^	x	X	X	X
weekOfMonth		X	X	×	X
weekOfYear		X	X	×	X
weekday		X	X	×	X
month		X	X	×	X
quarter		X	X	×	X
year		X	X	×	X
era		X	X	X	X
convertZoneRules		^	^	×	^
date			X	×	X
time			X	X	?
format	х	x	X	X	X
fromLeanTime24Hour	X	^	^	^	^
fromLean i ime24Hour fromTime12Hour	X				
fromTime12Hour fromTime24Hour	X				
	^	X			
fromAmericanDateString		x			
fromLeanDateString					
fromSQLDateString		х	v		V
fromAscTimeString			x x		Х
fromDateTimeString					
fromLeanDateTimeString			X		W.
fromLongDateFormatString			X		X
fromDateTimeWithZoneString				X	
fromISO8601String				×	
fromLeanDateTimeWithZoneString				x	
fromRFC822String				x	
fromRFC850String				x	
toLeanTime24Hour	Х				
toTime12Hour	Х				

56 toTime24Hour

1	=CONCATENAT		BitVec	UInt8	UInt16	UInt32	UInt64	USize	Int8	Int16	Int32	Int64	ISize
120	reduceZeroExte		X										
121	Signed arithme	tic											
122	abs		X						?	?	?	?	?
123	neg		X						Х	X	X	Х	Х
124	sdiv		X										
125	smod		X										
126	smtSDiv		X										
127	smtUDiv		X										
128	srem		X										
129	Unsigned arith	metic											
130	add	Х	X	Х	X	Х	Х	Х	Х	X	X	X	Х
131	div	Х		Х	X	Х	Х	Х	Х	X	Х	X	Х
132	mod	Х		Х	X	X	X	Χ	X	X	X	X	Х
133	udiv		X										
134	umod		X										
135	log2	Х		Х	X	Х	Х	Х					
136	modn	Х		X	X	X	X	X					
137	mul	Х	X	X	X	X	X	X	X	X	X	X	X
138	sub	Х	X	X	X	X	X	X	Х	X	X	X	Х
139	subNat	Х											
140	Bitwise operati	ons											
141	land	Х		X	Х	х	Х	х	Х	X	Х	Х	Х
142	and		X										
143	lor	Х		X	Х	Х	Х	Х	Х	X	X	Х	Х
144	or		X										
145	complement			Х	Х	X	X	Х	Х	X	X	X	Х
146	not		X										
147	хог	Х	X	Х	X	Х	Х	Х	Х	X	Х	X	Х
148	extractLsb		×										
149	extractLsb'		X										
150	reverse		X										
151	rotateLeft		×										
152	rotateLeftAux		X										
153	rotateRight		X										
154	rotateRightAux		X										
155	shiftConcat		X										
156	shiftLeft	Х	X	Х	X	Х	Х	Х	X	X	X	X	Х
157	shiftRight	Х		Х	х	x	x	Х	Х	х	х	х	Х
158	sshiftRight		X										
159	sshiftRight'		X										
160	ushiftRight		X										

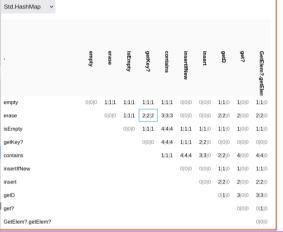
Next steps API Manager



Step 1: Associate operations across namespaces

Step 2: See which lemmas exist

Step 3: Check lemmas for consistency



```
Std.DHashMap.getKey?_erase.{u, v} {α : Type u} {β : α - Type v} {x† : BEq α} {x† : Hashable α} {m : Std.DHashMap αβ} [EquivBEq α] [LawfulHashable α] {k α : α} : (m.erase k).getKey? α = if (k == α) = true then none else m.getKey? α Std.DHashMap.getKey?_erase_self.{u, v} {α : Type u} {β : α - Type v} {x† : BEq α} {x† : Hashable α} {m : Std.DHashMap αβ} [EquivBEq α] [LawfulHashable α] {k : α} : (m.erase k).getKey? k = none

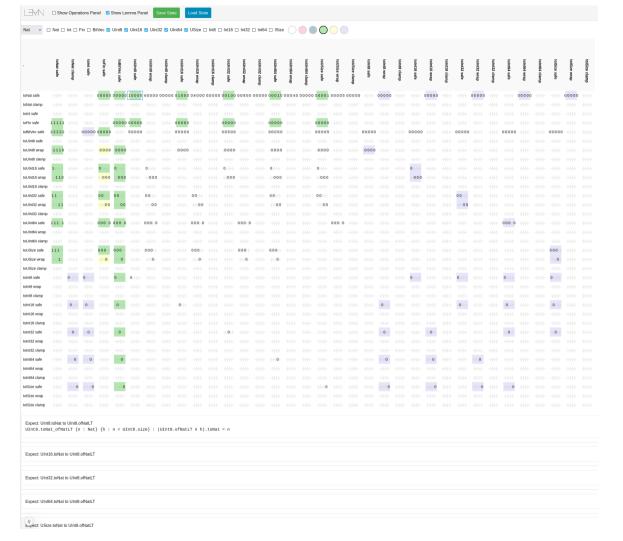
Std.HashMap.getKey?_erase_self.{u, v} {α : Type u} {β : Type v} {x† : BEq α} {x† : Hashable α} {m : Std.HashMap αβ} [EquivBEq α] [LawfulHashable α] {k : α} : (m.erase k).getKey? k = none

Std.HashMap.getKey?_erase.{u, v} {α : Type u} {β : Type v} {x† : BEq α} {x† : Hashable α} {m : Std.HashMap αβ} [EquivBEq α] [LawfulHashable α] {k α : α} : (m.erase k).getKey? α = if (k == α) = true then none else m.getKey? α

Std.HashSet.get?_erase.{u} {α : Type u} {x† : BEq α} {x† : Hashable α} {m : Std.HashSet α} [EquivBEq α] [LawfulHashable α] {k α : α} : (m.erase k).get? α = if (k == α) = true then none else m.getRey? α

Std.HashSet.get?_erase.self.{u} {α : Type u} {x† : BEq α} {x† : Hashable α} {m : Std.HashSet α} [EquivBEq α] [LawfulHashable α] {k : α} : (m.erase k).get? α = none
```

Next steps



Tool for tracking changes to the entire library

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Basic question: what do we know? (and when do we no longer know it?)

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Declaratively and imperatively describe the library and how it should look

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Web UI for analyzing the library

Tool for tracking changes to the entire library

Basic question: what do we know? (and when do we no longer know it?)

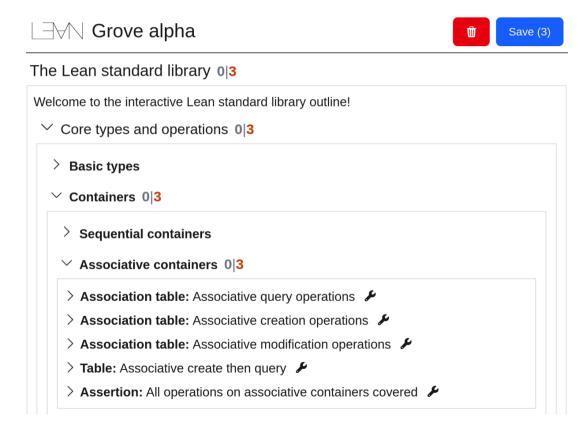
Declaratively and imperatively describe the library and how it should look

Full power of Lean metaprogramming for extracting state

Web UI for analyzing the library

Detects changes in PRs

```
def associativeContainers : List Lean.Name :=
  [`Std.DHashMap, `Std.DHashMap.Raw, `Std.ExtDHashMap, `Std.DTreeMap,
   `Std.DTreeMap.Raw, `Std.ExtDTreeMap, `Std.HashMap, `Std.HashMap.Raw,
   `Std.ExtHashMap, `Std.TreeMap, `Std.TreeMap.Raw, `Std.ExtTreeMap,
   `Std.HashSet, `Std.HashSet.Raw, `Std.ExtHashSet, `Std.TreeSet,
   `Std.TreeSet.Raw, `Std.ExtTreeSet]
def associativeQueryOperations : AssociationTable .subexpression associativeContainers where
  id := "associative-query-operations"
  title := "Associative guery operations"
  description := "Operations that take as input an associative container and return a 'single' pi
  dataSources n :=
    (DataSource.definitionsInNamespace n)
      |>.map Subexpression.declaration
      |>.or (DataSource.getElem n)
```



Grove alpha The Lean standard library / Core types and operations / Containers / Associative containers / Associative query operations

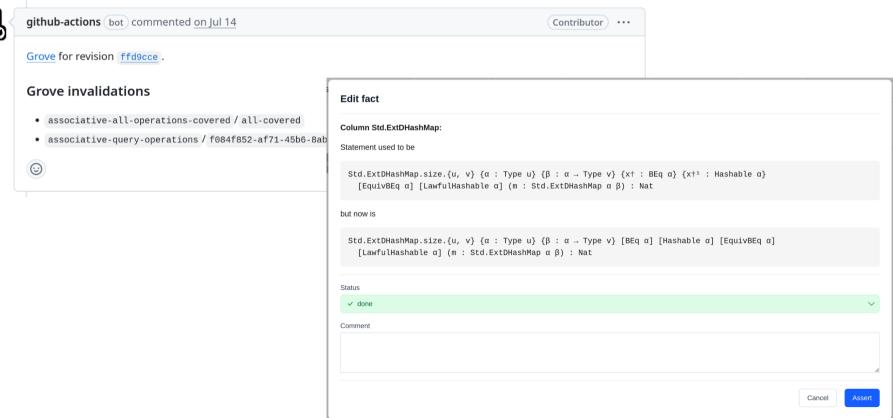
Title	Std.DHashMap	Std.DHashMap.Raw	Std.ExtDHashMap	Std.DTreeMap	Std.DTreeMap.Raw	Std.ExtDTreeMap	Std.HashMap	Std.HashMap.Raw
isEmpty	Std.DHashMap.isEmpty	Std.DHashMap.Raw.isEmpty	Std.ExtDHashMap.isEmpty	Std.DTreeMap.isEmpty	Std.DTreeMap.Raw.isEmpty	Std.ExtDTreeMap.isEmpty	Std.HashMap.isEmpty	Std.HashMap.Raw.isEmpty
size	Std.DHashMap.size	Std.DHashMap.Raw.size	Std.ExtDHashMap.size	Std.DTreeMap.size	Std.DTreeMap.Raw.size	Std.ExtDTreeMap.size	Std.HashMap.size	Std.HashMap.Raw.size
any				Std.DTreeMap.any	Std.DTreeMap.Raw.any	Std.ExtDTreeMap.any		
all				Std.DTreeMap.all	Std.DTreeMap.Raw.all	Std.ExtDTreeMap.all		
getD	Std.DHashMap.getD	Std.DHashMap.Raw.getD	Std.ExtDHashMap.getD	Std.DTreeMap.getD	Std.DTreeMap.Raw.getD	Std.ExtDTreeMap.getD	Std.HashMap.getD	Std.HashMap.Raw.getD
getElem	Std.DHashMap.get	Std.DHashMap.Raw.Const.get	Std.ExtDHashMap.get	Std.DTreeMap.get	Std.DTreeMap.Raw.get	Std.ExtDTreeMap.get	Std.HashMap[·]	Std.HashMap.Raw[·]
isSingleton						Std.ExtDTreeMap.isSingleton		

	isEmpty	size	getD	getElem
empty	3 3 0 2 2 0	1 1 0 0 0 0	1 1 0 0 0 0	0 0 0 0 0
ofList	1 1 0 0 0 0	2 2 2 1 1 2	2 2 2 2 2 2	1 0 1 1 1 1
emptyCollection	6 5 3 1 1 3	2 2 5 1 1 5	2 2 1 2 0 1	0 0 2 0 0 0









```
widgetId := "associative-create-then-query"
 factId := "5ceaa26a-d2cb-4df3-9ac8-b5c11db2ae9d:::01f88623-fa5f-4380-9772-b30f2fec5c94:::Std.DHashMap::Std.DHashMap:Raw::Std.ExtDHashMap::Std.DTreeMap:Raw::
 rowAssociationId := "5ceaa26a-d2cb-4df3-9ac8-b5c11db2ae9d"
 columnAssociationId := "01f88623-fa5f-4380-9772-b30f2fec5c94"
 selectedLayers := #["Std.DHashMap", "Std.DHashMap,Raw", "Std.ExtDHashMap", "Std.DTreeMap", "Std.DTreeMap.Raw", "Std.ExtDTreeMap", ]
 laverStates := #[
     laverIdentifier := "Std.DHashMap"
     rowState :=
      some ("app (EmptyCollection.emptyCollection) (Std.DHashMap*)", Grove.Framework.Subexpression.State.predicate
       { kev := "app (EmptyCollection.emptyCollection) (Std.DHashMap*)", displayShort := "∅" })
     columnState :=
      some ("Std.DHashMap.isEmpty", Grove.Framework.Subexpression.State.declaration
        (Grove.Framework.Declaration.def
          { name := `Std.DHashMap.isEmptv.
            renderedStatement := "Std.DHashMap.isEmpty.{u, v} {\alpha : Type u} {\beta : \alpha - Type v} {xt : BEq \alpha} {xt' : Hashable \alpha}\n (m : Std.DHashMap \alpha \beta) : Bool",
            isDeprecated := false }))
     selectedCellStates := #[
      ("Std.DHashMap.isEmpty_empty", Grove.Framework.Declaration.thm
  { name := `Std.DHashMap.isEmpty_empty,
   renderedStatement := "Std.DHashMap.isEmpty empty.{u, v} {α : Type u} {β : α → Type v} {x† : BEq α} {x† : Hashable α} :\n Ø.isEmpty = true",
   isSimp := true.
   isDeprecated := false }>
     laverIdentifier := "Std.DHashMap.Raw"
      some ("app (EmptyCollection.emptyCollection) (Std.DHashMap.Raw*)", Grove.Framework.Subexpression.State.predicate
       { key := "app (EmptyCollection.emptyCollection) (Std.DHashMap.Raw*)", displayShort := "⊘" })
     columnState :=
       some ("Std.DHashMap.Raw.isEmpty", Grove.Framework.Subexpression.State.declaration
        (Grove.Framework.Declaration.def
          { name := `Std.DHashMap.Raw.isEmpty,
            renderedStatement := "Std.DHashMap.Raw.isEmpty.{u, v} {α : Type u} {β : α - Type v} (m : Std.DHashMap.Raw α β) : Bool",
            isDeprecated := false }))
     selectedCellStates := #[
      ("Std.DHashMap.Raw.isEmpty_emptyc", Grove.Framework.Declaration.thm
 { name := `Std.DHashMap.Raw.isEmpty_emptyc,
   renderedStatement := "Std.DHashNap.Raw.isEmpty_emptyc.{u_1, u_2} {α : Type u_1} {β : α - Type u_2} [BEq α] [Hashable α] :\n Ø.isEmpty = true",
   isSimp := false.
   isDeprecated := true })
     layerIdentifier := "Std.ExtDHashMap"
     rowState :=
      some ("app (EmptyCollection,emptyCollection) (Std.ExtDHashMap*)", Grove.Framework.Subexpression.State.predicate
```

